

$\forall x \in \mathbb{R} - \left\{ \frac{\pi}{2} + k\pi / k \in \mathbb{Z} \right\}$ $\tan(-x) = -\tan(x)$ $\tan(\pi - x) = -\tan(x)$ $\tan(\pi + x) = \tan(x)$ $\tan\left(\frac{\pi}{2} - x\right) = \frac{1}{\tan(x)} / x \neq 0 [2\pi]$ $\tan\left(\frac{\pi}{2} + x\right) = -\frac{1}{\tan(x)} / x \neq 0 [2\pi]$	$\forall x \in \mathbb{R}$ $\sin(-x) = -\sin(x)$ $\sin(\pi - x) = \sin(x)$ $\sin(\pi + x) = -\sin(x)$ $\sin\left(\frac{\pi}{2} - x\right) = \cos(x)$ $\sin\left(\frac{\pi}{2} + x\right) = \cos(x)$	$\forall x \in \mathbb{R}$ $\cos(-x) = \cos(x)$ $\cos(\pi - x) = -\cos(x)$ $\cos(\pi + x) = -\cos(x)$ $\cos\left(\frac{\pi}{2} - x\right) = \sin(x)$ $\cos\left(\frac{\pi}{2} + x\right) = -\sin(x)$
$\tan(x) = \frac{\sin(x)}{\cos(x)}$ $1 + \tan^2(x) = \frac{1}{\cos^2(x)}$ $\cotan(x) = \frac{1}{\tan(x)}$ $\sin^2(x) = \frac{\tan^2(x)}{1 + \tan^2(x)}$	$-1 \leq \sin \leq 1$ $\sin(x + 2k\pi) = \sin(x)$ $\sin(x + k\pi) = (-1)^k \sin(x)$ $\sin\left(n\frac{\pi}{2}\right) = (-1)^n$	$-1 \leq \cos \leq 1$ $\cos(x + 2k\pi) = \cos(x)$ $\cos(x + k\pi) = (-1)^k \cos(x)$ $\cos(n\pi) = (-1)^n$
	$\cos^2(x) + \sin^2(x) = 1$	
$\tan(a+b) = \frac{\tan(a) + \tan(b)}{1 - \tan(a).\tan(b)}$ $\tan(a-b) = \frac{\tan(a) - \tan(b)}{1 + \tan(a).\tan(b)}$	$\cos(a+b) = \cos(a)\cos(b) - \sin(a)\sin(b)$ $\cos(a-b) = \cos(a)\cos(b) + \sin(a)\sin(b)$ $\sin(a+b) = \sin(a)\cos(b) + \cos(a)\sin(b)$ $\sin(a-b) = \sin(a)\cos(b) - \cos(a)\sin(b)$	
$\tan(a) + \tan(b) = \frac{\sin(a+b)}{\cos(a).\cos(b)}$ $\tan(a) - \tan(b) = \frac{\sin(a-b)}{\cos(a).\cos(b)}$	$\cos(a)\cos(b) = \frac{1}{2}[\cos(a+b) + \cos(a-b)]$ $\sin(a)\sin(b) = \frac{1}{2}[\cos(a-b) - \cos(a+b)]$ $\sin(a)\cos(b) = \frac{1}{2}[\sin(a+b) + \sin(a-b)]$	
$\cos(2a) = \cos^2(a) - \sin^2(a)$ $= 2\cos^2(a) - 1$ $= 1 - 2\sin^2(a)$ $\sin(2a) = 2\sin(a)\cos(a)$ $\tan(2a) = \frac{2\tan(a)}{1 - \tan^2(a)}$	$\cos(a) + \cos(b) = 2\cos\left(\frac{a+b}{2}\right)\cos\left(\frac{a-b}{2}\right)$ $\cos(a) - \cos(b) = -2\sin\left(\frac{a+b}{2}\right)\sin\left(\frac{a-b}{2}\right)$ $\sin(a) + \sin(b) = 2\sin\left(\frac{a+b}{2}\right)\cos\left(\frac{a-b}{2}\right)$ $\sin(a) - \sin(b) = 2\sin\left(\frac{a-b}{2}\right)\cos\left(\frac{a+b}{2}\right)$	

$$t = \tan\left(\frac{x}{2}\right) \quad \text{إذا وضد هنا}$$

$$\cos(x) = \frac{1-t^2}{1+t^2} \quad : \quad \text{فإن}$$

$$\sin(x) = \frac{2t}{1+t^2} \quad \text{و}$$

$$\tan x = \frac{2t}{1-t^2} \quad \text{و}$$

$$1 + \cos(a) = 2 \cos^2\left(\frac{a}{2}\right)$$

$$1 - \cos(a) = 2 \sin^2\left(\frac{a}{2}\right)$$

$$\sin(a) = 2 \sin\left(\frac{a}{2}\right) \cos\left(\frac{a}{2}\right)$$

$$\cos^2(a) = \frac{1 + \cos(2a)}{2}$$

$$\sin^2(a) = \frac{1 - \cos(2a)}{2}$$

$$\tan^2(a) = \frac{1 - \cos(2a)}{1 + \cos(2a)}$$

$$\sin(x) = \sin(\alpha) \Leftrightarrow \begin{cases} x = \alpha + 2k\pi \\ \text{أو} \\ x = \pi - \alpha + 2k\pi \end{cases} / k \in \mathbb{Z}$$

$$\cos(x) = \cos(\alpha) \Leftrightarrow \begin{cases} x = \alpha + 2k\pi \\ \text{أو} \\ x = -\alpha + 2k\pi \end{cases} / k \in \mathbb{Z}$$

$$a \cos(x) + b \sin(x) = \sqrt{a^2 + b^2} \sin(x + \alpha)$$

$$\begin{cases} \sin(\alpha) = \frac{a}{\sqrt{a^2 + b^2}} \\ \cos(\alpha) = \frac{b}{\sqrt{a^2 + b^2}} \end{cases} \quad \text{حيث: و}$$

$$a \cos(x) + b \sin(x) = \sqrt{a^2 + b^2} \cos(x - \alpha)$$

$$\begin{cases} \cos(\alpha) = \frac{a}{\sqrt{a^2 + b^2}} \\ \sin(\alpha) = \frac{b}{\sqrt{a^2 + b^2}} \end{cases} \quad \text{حيث: و}$$

$$\tan(x) = \tan(\alpha) \Leftrightarrow x = \alpha + k\pi / k \in \mathbb{Z}$$

x	π	$\frac{5\pi}{6}$	$\frac{3\pi}{4}$	$\frac{2\pi}{3}$	$\frac{\pi}{2}$	$\frac{\pi}{3}$	$\frac{\pi}{4}$	$\frac{\pi}{6}$	0
$\sin(x)$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
$\cos(x)$	-1	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
$\tan(x)$	0	$-\frac{\sqrt{3}}{3}$	-1	$-\sqrt{3}$	$\frac{\text{غير معروف}}{\text{معروف}}$	$\sqrt{3}$	1	$\frac{\sqrt{3}}{3}$	0